

COM 501 Advanced Datastructures and Algorithms **Assignment-2** Due: Feb 2

Use Substitution/recursion tree/guess/Master theorem to solve the following recurrence relations to get asymptotic upper bounds.

1.  $T(n) = 3T(n/2) + n$ .
2.  $T(n) = 8T(n/2) + n \log n$
3.  $T(n) = 9T(n/3) + n^2 \log n$
4. Use a recursion tree to give an asymptotically tight solution to the recurrence  $T(n) = T(\alpha n) + T((1 - \alpha)n) + cn$ , where  $\alpha$  is a constant in the range  $0 < \alpha < 1$  and  $c > 0$  is also a constant.
5. Solve:  $T(n) = \sqrt{T(n-1) \times T(n-2)}$
6. Solve.  $T(n) = T(\frac{n}{2} + 5) + n$ ,  $T(1) = 1$
7. Solve.  $T(n) = n.T(n-1) + n(n-1)T(n-2)$ ,  $T(1) = 1, T(2) = 2$