

Discrete Mathematics - Problem Session -1

1. united we stand, divided we fall:  $P \wedge Q$
2. Someone is sitting in the shade today because someone planted a tree a longtime ago:  $\exists x(\text{sitshade}(x)) \wedge \exists y(\text{planttree}(y))$
3. If you spend your life trying to be good at everything, you will never be great at anything:  $\forall x(\text{person}(x) \rightarrow (\forall y(\text{thing}(y) \rightarrow \text{goodat}(x, y)) \rightarrow \forall y(\text{thing}(y) \rightarrow \neg \text{greatat}(x, y))))$
4. Everybody wants to go to heaven, but nobody wants to die:  $\forall x(H(x)) \wedge \neg \exists x(D(x))$
5. Research is to see what everybody else has seen, and to think what nobody else has thought.:  $\text{Research} \rightarrow (\forall x(\text{seen}(x) \wedge \text{think}(x) \rightarrow \forall y(y \neq x \rightarrow \text{seen}(y) \wedge \neg \text{think}(y))))$
6. Everyone wants to walk in shade but no one wants to plant trees.:  $\forall x(S(x)) \wedge \neg \exists x(P(x))$
7. A person who never made a mistake never tried anything new:  $\forall x((\text{person}(x) \wedge \neg \text{mistake}(x)) \rightarrow \forall y(\text{newthing}(y) \rightarrow \neg \text{try}(x, y)))$
8. True knowledge exists in knowing that you know nothing:  $P$
9. If Aug 15 is a holiday, then some students of IIITDM will go home and the rest will solve DM assignment.  $P \rightarrow (\exists x(\text{home}(x) \wedge \forall y(y \neq x \rightarrow \text{DM}(y))))$
10. Write in FOL: There exists at most one  $x$  such that  $P(x)$ . :  $\neg \exists x P(x) \vee \exists! x P(x)$
11. Write in FOL: There exists at least three  $x$  such that  $P(x)$ :  $\exists x \exists y \exists z (x \neq y \neq z \wedge P(x))$
12. Some thing that is white is not always milk, whereas the milk is always white.  $\exists x(W(x) \wedge \neg M(x)) \wedge \forall x(M(x) \rightarrow W(x))$
13. Each student of IIITDM likes either carnatic music or Hindustani music. Further, some students are athletes, however, they have not represented the institute in inter sports meet. Carnatic music is a form of meditation. Music club at IIITDM is not that active. Therefore, students of IIITDM are neither good in sports nor in music. :  $(\forall x(C(x) \oplus H(x)) \wedge \exists x(A(x) \wedge \neg I(x)) \wedge C \wedge \neg M) \rightarrow \forall x(\neg S(x) \wedge \neg M(x))$
14. Since it is a Monday, all are back to work.:  $M \wedge \forall x(B(x))$
15. While I was walking along the corridor, I met him in the mid way.:  $P \wedge Q$
16. As the semester is in full swing, students hardly find time for entertainment.:  $P \wedge Q$